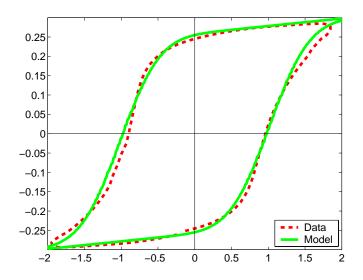
# A UNIFIED MODEL FOR HYSTERESIS IN FERROIC MATERIALS

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- Stefan Seelecke, North Carolina State University



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#### TALK OVERVIEW

# I. Smart Material Applications

- Piezoelectrics Tunable lenses, nanopositioning
- Shape Memory Alloys Shape modification
- Magnetostrictives High force transduction

### **II. Modeling Hierarchies**

- Develop energy relations at lattice level for single crystal, homogeneous compounds.
- Incorporate polycrystallinity and material nonhomogeneities through stochastic homogenization to obtain macroscopic constitutive relations.

#### III. Experimental Validation

- PZT5A Major and biased minor loops
- Terfenol-D Major and biased minor loops
- SMA Thin film

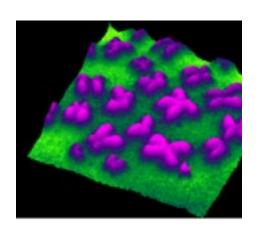
#### Goal:

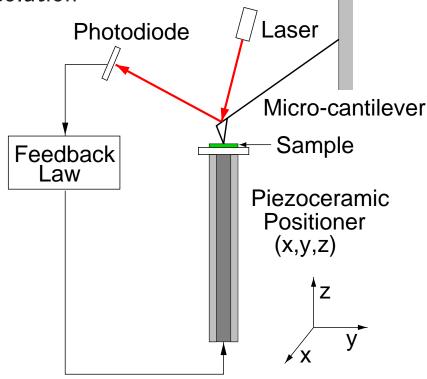
 Develop a unified framework for model and control design for ferroic (ferromagnetic, ferroelectric and ferroelastic) materials.

#### I. PIEZOCERAMICS - NANOPOSITIONING

#### **Atomic Force Microscope:**

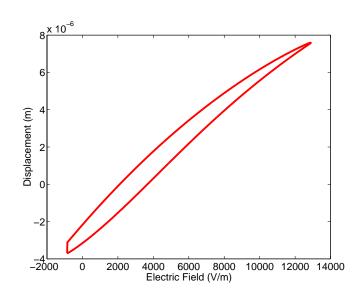
- Can provide atomic resolution
- Human chromosomes





# **Model Development:**

- Must be able to attain Angstrom-level resolution
- Must be implemented in real time



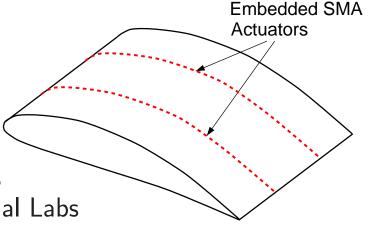
# **Future Capabilities:**

- Nanopositioning at the atomic level
- Electron spin detection: requires angstrom-level tracking

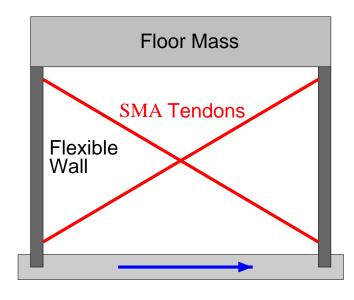
#### SHAPE MEMORY ALLOYS

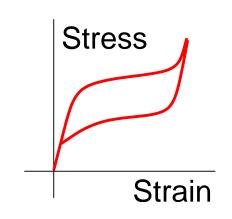
# **Aerospace and Aeronautic Applications:**

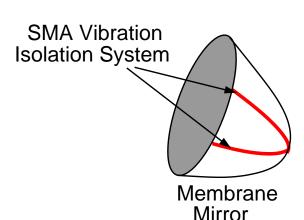
- Shape modification of airfoils
- Construction of modular mirrors and antennas
- Future Directions: MEM's,
   thin films Sandia National Labs



#### **Vibration Attenuation:**





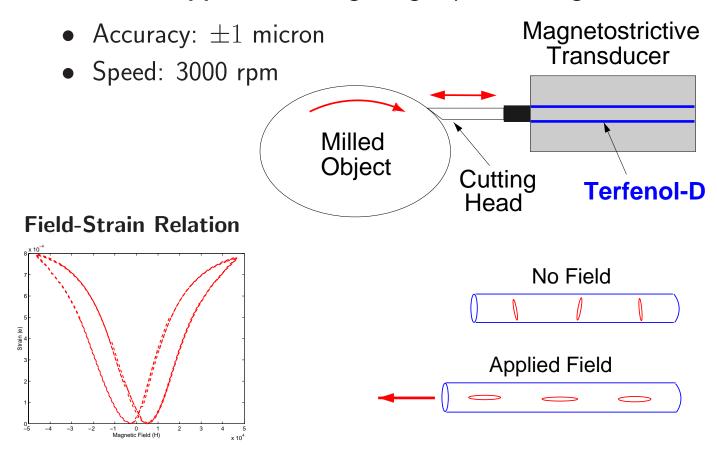


# **Strategy:**

- Vibration attenuation in aerospace structures (e.g., mirrors)
- Operate in hysteretic regime to optimize damping

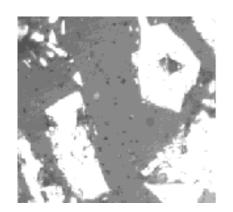
#### **MAGNETOSTRICTIVE MATERIALS**

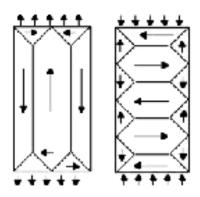
Automotive Application: e.g., High speed milling



# **Aerospace Applications:**

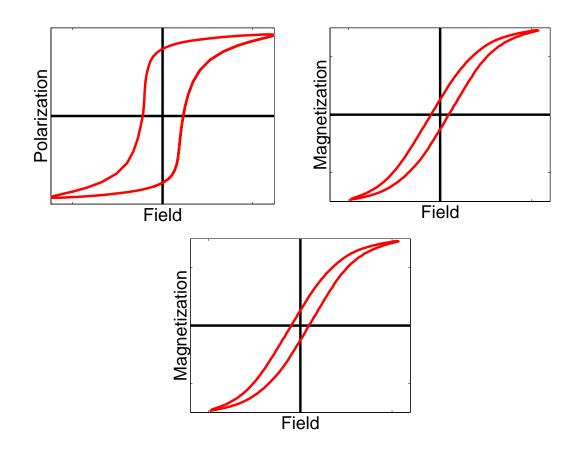
• Magnetostrictive composites for active structural damping





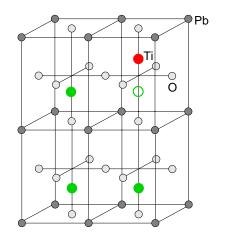
# **MATERIAL ANALOGIES**

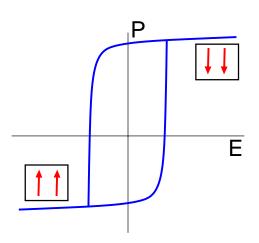
Ferroelectric	Ferromagnetic	Ferroelastic	
Polarization	Magnetization	Strain	
Electric field	Magnetic field	Stress	
Paraelectric phase	Paramagnetic phase	Austenite phase	
Ferroelectric phase	Ferromagnetic phase	Martensite phase	
Ferroelectric domain walls	Bloch or Neel walls	Boundaries between martensite variants	
Devonshire theory	Mean field (Weiss) theory	Landau theory	
	Micromagnetic theory	Ginzburg-Landau theory	



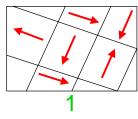
### MECHANISMS WHICH PRODUCE HYSTERESIS

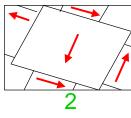
Ferroelectric: Dipole switching

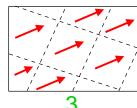


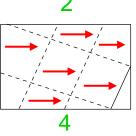


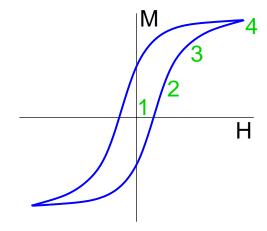
Ferromagnetic: Moment rotation, domain wall losses



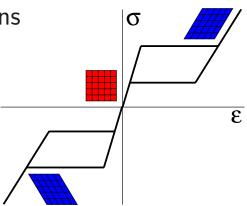




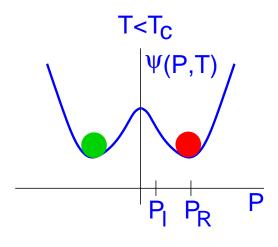


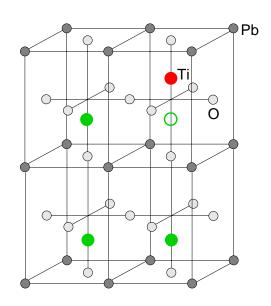


Ferroelastic: Phase transitions



#### MESOSCOPIC MODEL - HELMHOLTZ ENERGY





# Helmholtz Energy:

$$\psi(P,T) = U - ST$$

$$= \frac{\Phi_0 N}{4V} [1 - (P/P_s)^2] + \frac{TkN}{2VP_s} \left[ P \ln \left( \frac{P + P_s}{P_s - P} \right) + P_s \ln(1 - (P/P_s)^2) \right]$$

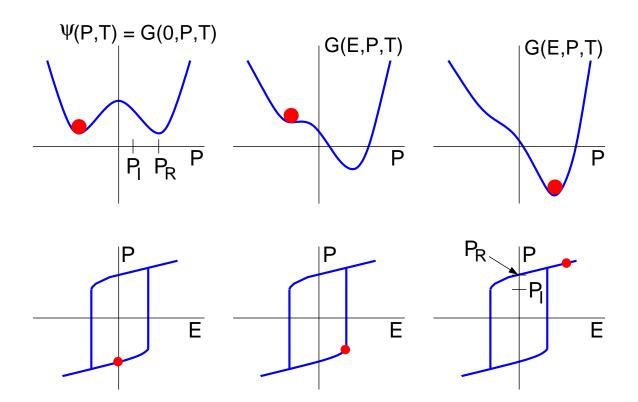
# **Helmholtz Energy Relations:**

$$\psi(P) = \begin{cases} \frac{\eta}{2} (P \pm P_R)^2 &, |P| \ge P_I \\ \frac{\eta}{2} (P_I - P_R) \left[ \frac{P^2}{P_I} - P_R \right] &, |P| < P_I \end{cases}$$

$$\psi(M) = \begin{cases} \frac{\eta}{2} (M \pm M_R)^2 &, |M| \ge M_I \\ \frac{\eta}{2} (M_I - M_R) \left[ \frac{M^2}{M_I} - M_R \right] &, |M| < M_I \end{cases}$$

$$\psi(\varepsilon,T) = \begin{cases} \frac{E_M}{2} (\varepsilon \pm \varepsilon_T)^2 &, |\varepsilon| \ge \gamma_M(T) \\ -\frac{E_0(T)}{2} [\varepsilon \pm \varepsilon_0(T)]^2 + \psi_0(T) &, |\gamma_A(T)| < \varepsilon < |\gamma_M(T)| \\ \frac{E_A}{2} \varepsilon^2 + \Delta \beta(T) &, |\varepsilon| \le \gamma_A(T) \end{cases}$$

#### **MESOSCOPIC MODEL – GIBBS ENERGY**



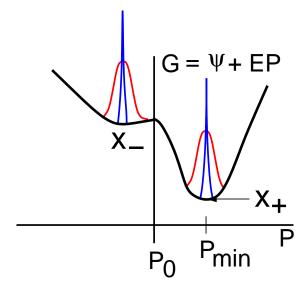
# **Gibbs Energy Relations:**

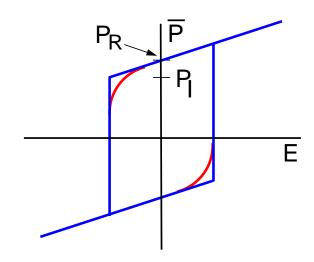
$$G(E, P, T) = \psi(P, T) - EP$$
 (Ferroelectric)

$$G(H, M, T) = \psi(M, T) - \mu_0 HM$$
 (Ferromagnetic)

$$G(\sigma, \varepsilon, T) = \psi(\varepsilon, T) - \sigma\varepsilon$$
 (Ferroelastic)

#### **MESOSCOPIC MODELS – UNIFORM LATTICE**





# **Boltzmann Probability:**

$$\mu(G) = Ce^{-GV/kT} \implies p_{+-} = \sqrt{\frac{kT}{2\pi mV^{2/3}}} \cdot \frac{e^{-G(E,P_0(T),T)V/kT}}{\int_{P_0}^{\infty} e^{-G(E,P,T)V/kT} dP}$$

#### **Evolution Relations:**

$$\frac{dx_+}{dt} = -p_{+-}x_+ + p_{-+}x_-$$
 
$$\frac{dx_-}{dt} = -p_{-+}x_- + p_{+-}x_+$$
 Ferroelastic: Analogous

#### **Polarization:**

$$\overline{P} = x_+ \langle P_+ \rangle + x_- \langle P_- \rangle$$

where

$$\langle P_{+} \rangle = \int_{P_{0}}^{\infty} P \mu(G) dP$$

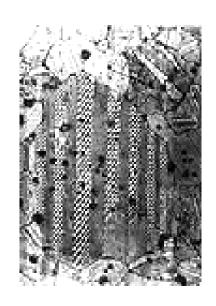
# **Magnetization:**

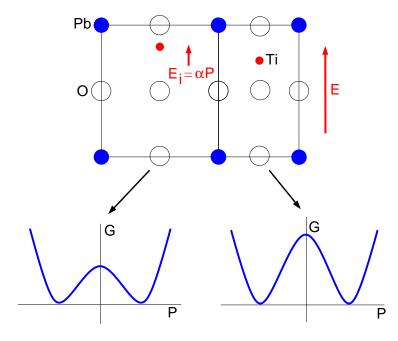
$$\overline{M} = x_+ \langle M_+ \rangle + x_- \langle M_- \rangle$$

where

$$\langle M_+ \rangle = \int_{M_0}^{\infty} M \mu(G) dM$$

#### MACROSCOPIC MODELS



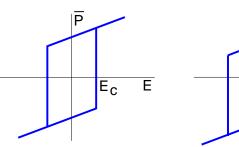


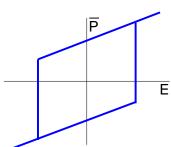
#### **Nonuniform Lattice:**

$$f(E_c) = C_1 e^{-[\ln(E_c/\overline{E}_c)/2b]^2}$$

# Variable Effective Fields:

$$\widehat{f}(\mathcal{E}) = C_2 e^{-(\mathcal{E} - E)^2/\bar{b}}$$





#### **Macroscopic Models:**

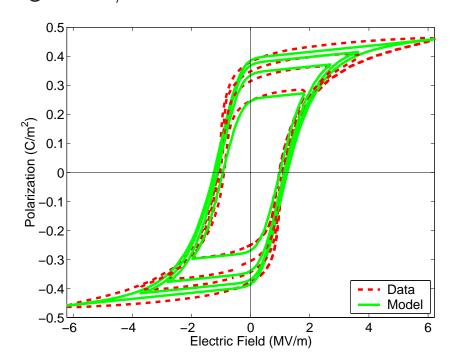
$$[P(E,T)](t) = C \int_0^\infty \int_{-\infty}^\infty f(E_c) \widehat{f}(\mathcal{E}) [\overline{P}(\mathcal{E}+E,T)](t) d\mathcal{E} dE_c$$

$$[M(H,T)](t) = C \int_0^\infty \int_{-\infty}^\infty f(H_c) \widehat{f}(\mathcal{H}) [\overline{M}(\mathcal{H} + H, T)](t) d\mathcal{H} dH_c$$

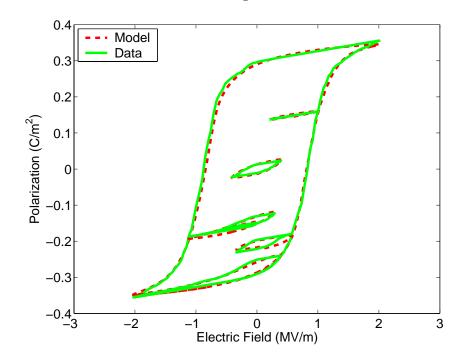
$$[\varepsilon(\sigma,T)](t) = C \int_0^\infty \int_{-\infty}^\infty f(\delta) \widehat{f}(\sigma_E) [\overline{\varepsilon}(\sigma_E + \sigma,T)](t) d\sigma_E d\delta$$

### III. EXPERIMENTAL VALIDATION

**PZT5A:** Lognormal/normal densities

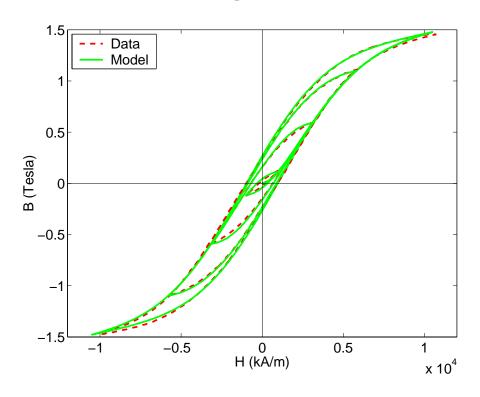


PZT5A: ID of general densities [B. Mukherjee, S-F. Liu - Data]

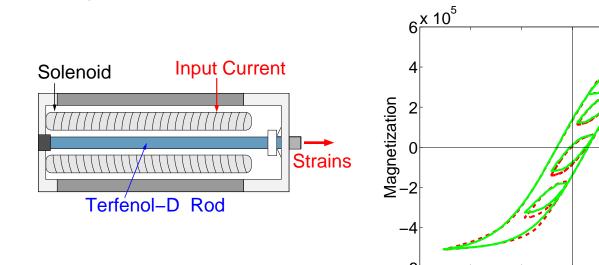


### **VALIDATION – FERROMAGNETIC MATERIALS**

Example 1: Steel data from [Jiles and Atherton; 1984]



**Example 2:** Terfenol-D Transducer



Data Model

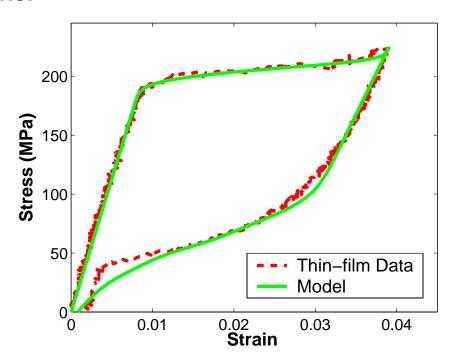
0 Field

2

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# **EXPERIMENTAL VALIDATION - SMA**

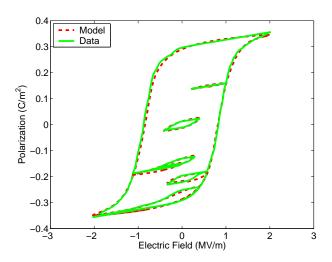
# Thin Films:

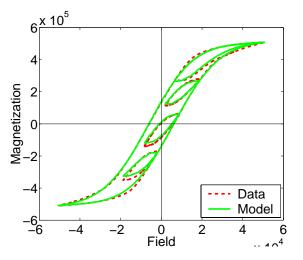


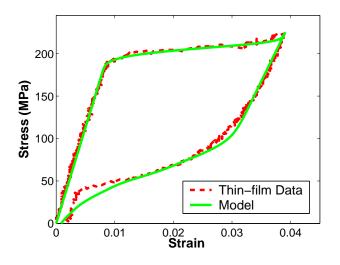
# **CONCLUDING REMARKS**

#### Model Attributes:

- (1) Technique provides unified framework for modeling hysteresis in ferroelectric, ferromagnetic and ferroelastic materials.
- (2) Low number (5-10) and physical nature of parameters facilitates parameter estimation and control implementation.
- (3) Model guarantees closure of biased minor loops.
- (4) Model is amenable to inversion which facilitates linear control design.
- (5) Method provides energy basis for Preisach models.







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